

M.E. First Semester (Electrical & Elect.) (New-CGS)  
**13281 : Advanced Control Systems : 1 EEEME 1**

P. Pages : 3

Time : Three Hours



AU - 3396

Max. Marks : 80

- Notes :
1. All question carry equal marks.
  2. Answer **three** question from Section A and **three** question from Section B.
  3. Use of pen Blue/Black ink/refill only for writing the answer book.

**SECTION - A**

1. Find  $y(k)$  for given equation  $y(k) = r(k) - r(k-1) - y(k-1)$ ,  $k \geq 0$  13  
 where  

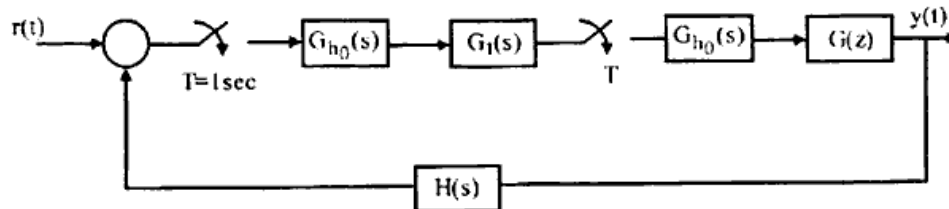
$$r(k) = \begin{cases} 1 & k \text{ is even} \\ 0 & k \text{ is odd} \end{cases}$$
  
 $y(-1) = r(-1) = 0$ .

**OR**

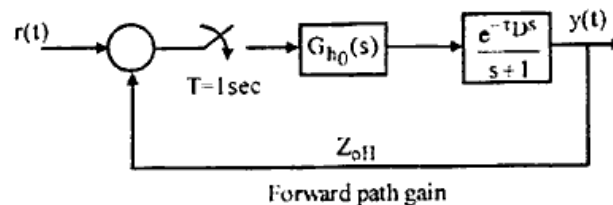
2. Consider a discrete time system described by the differential equation. 13  

$$y(k+2) + \frac{1}{4}y(k+1) - \frac{1}{8}y(k) = 3r(k+1) - r(k)$$
  
 The system is relaxed  $y(k) = 0$ ,  $k < 0$  and is excited by the input  $r(k) = (-1)^k u(k)$  obtained T.k model of discrete time system and hence find the output  $y(k)$ ;  $k > 0$ .

3. a) Find  $Y(z)/R(z)$  for the input data closed loop system. 6



- b) Consider the sample data system shown. find  $Y(z)/R(z)$  when  $T_D = 0.4 \text{ sec}$ . 8



**OR**

4. a) A unity feedback system has open loop transfer function. 6  

$$G(s) = \frac{5}{s(s+1)(s+2)}$$
  
 using Routh stability criteria show that closed loop system is stable.

- b) Consider the digital controller defined by

8

$$D(z) = \frac{u(z)}{E(z)} = \frac{10(z^2 + z + 1)}{z^2(z - 0.5)(z - 0.8)}$$

Draw the parallel realization.

5. Consider the control system in Fig. 5 the plant transfer func is

13

$$G(s) = \frac{1}{s(s+2)} \text{ and } T = 0.1 \text{ sec.}$$

- Increase plant gain value that results in  $k_v = 5$ . Then find phase margin.
- Design a lead compensator that results in  $55^\circ$  phase margin with  $k_v = 5$
- Design a lag compensator that results in  $55^\circ$  phase margin with  $k_v = 5$ .
- Obtain band with realized from the designs corresponding to (a), (b), (c)
- Is the selection of  $T=0.1$  sec justified from closed loop bandwidth considerations.

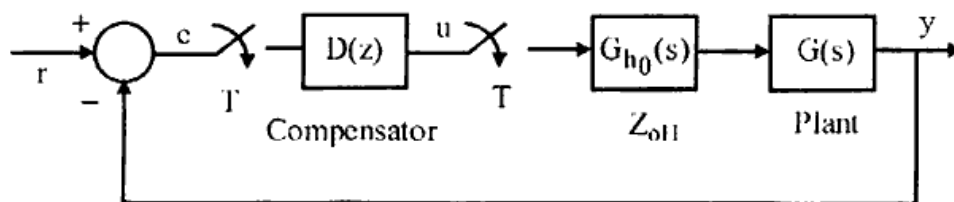


Fig. 5

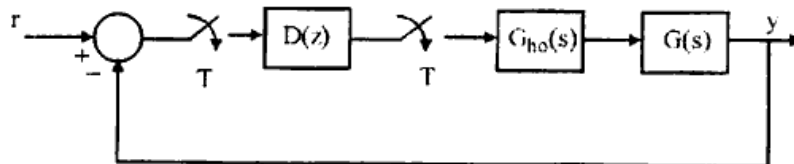
6. Consider the feedback control system shown in fig. The plant is described by the Tf

13

$$G(s) = \frac{k}{s(s+2)}$$

Design a digital is for the system to meet the fell. specifications.

- Velocity error const  $k_0 = 6$ .
- Peak overshoot  $M_p$  to step i/p  $\leq 15\%$
- Settling time  $t_s$  (2% tolerance band)  $\leq 5$  sec.



A feedback system using digital compensation

## SECTION - B

7. In following, realize three different form.

13

$$G(s) = \frac{s+3}{s^3 + 9s^2 + 24s + 20} = \frac{y(s)}{u(s)}$$

OR

8. a) Find T/F for given model.

5

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$$

$$y = [1 \quad 0] x$$

- b) Derive 2-state model for the system with 8  
 T.f  $\frac{y(s)}{u(s)} = \frac{50(1+s/5)}{s(1+s/2)(1+s/50)}$   
 for which system matrix is a companion form matrix.

9. a) State properties of STM in discrete system. 6

- b) Find whether the system 8  
 $u(k+1) = A x(k) + B u(k)$   
 $y(k) = c x(k)$   
 $A = \begin{bmatrix} 1 & -2 \\ 1 & -1 \end{bmatrix}$   $B = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$   $C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$   
 is controllable.

OR

10. a) Find state model of system. 8  
 $y(k+3) + 5y(k+2) + 7y(k+1) + 3y(k) = 0.$

- b) Derive necessary conditions for digital control system to be controllable. 6

11. Consider the system 13  
 $\dot{x} = Ax + Bu.$   
 $y = cx + du.$   
 where  
 $A = \begin{bmatrix} -2 & -1 \\ 1 & 0 \end{bmatrix}; B = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}; C = [0 \ 1], D = [2 \ 0]$   
 Design a full order state observer so that the estimation error will decay in less than 4 seconds.

OR

12. Consider a plant defined by the foll. State variable model. 13

$$x(k+1) = F x(k) + G u(k);$$

$$y(k) = c x(k) + d u(k)$$

where

$$F = \begin{bmatrix} 1/2 & 1 & 0 \\ -1 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}; G = \begin{bmatrix} 1 & 4 \\ 0 & 0 \\ -3 & 2 \end{bmatrix}; C = [1 \ 0 \ 0]; d = [0 \ 4]$$

Design a prediction observer for estimation of state vector  $x$ . The observer error poles are required to lie at  $-1/2 \pm j 1/4$ . Give all the relevant observer eq<sup>ns</sup> & block diag description of observer structure.

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