



- Notes :
1. All question carry marks as indicated.
 2. Assume suitable data wherever necessary.
 3. Use of pen Blue/Black ink/refill only for writing the answer book.

1. a) Explain : 8
- i) Propositional Calculus
 - ii) Set theory
 - iii) Quantifiers
- b) What is Asymptotic notation? Explain big O, theta notations in detail. 6

OR

2. a) Explain efficiency of algorithm and why do look for efficiency. 7
- b) Explain :
- i) Maximum Rule.
 - ii) Duality Rule.
 - iii) Threshold Rule.
3. a) Explain : 6
- i) Queue
 - ii) Records and pointers
- b) Prove that heap sort algorithm takes a time in $O(n \log n)$ to sort 'n' elements. 7

OR

4. a) Explain the analysis of algorithm using the barometer instruction. 7
- b) Solve the following recurrence by Intelligent Guesswork : 6

$$T(n) = \begin{cases} 0 & \text{if } n = 0 \\ 3T(n/2) + n & \text{otherwise} \end{cases}$$

5. a) What is divide and conquer? Explain with example. 7

- b) Explain Knapsack algorithm with example? 6
 $N = 3, m = 20$
 $(V_1, V_2, V_3) = (25, 24, 15)$
 $(W_1, W_2, W_3) = (18, 15, 10)$

OR

6. a) Explain Exponentiation as an example of divide and conquer. 7
 b) Prove that quick sort takes a time $O(n \log n)$ to sort n elements on the average. 6
7. a) Explain Recursion with suitable example. 7
 b) Explain the chain matrix multiplication algorithm for dynamic programming. 7

OR

8. Use Branch and Bound technique to solve the assignment problem with the following cost matrix. 14

task Agent	1	2	3	4
a	11	12	18	40
b	14	15	13	22
c	11	17	19	23
d	17	14	20	28

9. a) Explain parallel merging networks in brief. 6
 b) Prove that "A Sorting Network with ' n ' inputs correctly sort any set of values on its inputs if and only if it correctly sort all the $2n$ inputs vector consisting only zero and one". 7

OR

10. a) Explain Monte Carlo algorithm in detail. 7
 b) Describe parallel algorithm to find the connected component of the graph with suitable example. 6
11. a) What is Heuristic algorithm. Explain with example. 7
 b) Prove that $MQ \leq IT$, assuming IT is smooth. 6

OR

12. a) Prove that any binary tree with K leaves has an average height of at least $\lg K$. 7
 b) Explain in brief NP – hard problems. 6
