

## B.C.A. (Part-I) Semester-II Examination

## NUMERICAL METHODS

## Paper—2ST4

Time : Three Hours]

[Maximum Marks : 60

**Note :—**(1) All questions carry equal marks.

(2) All questions are compulsory.

1. (a) Explain method of least square regression. 4

(b) Fit a multiple linear regression to the following data :

 $x_1$ : 0 2 2.5 1 4 7 $x_2$ : 0 1 2 3 6 2

y: 5 10 9 0 3 27 4

(c) State the normal equation for fitting a second degree parabola. 4

**OR**

2. (a) Explain scatter diagram in detail. 4

(b) Fit a straight line to the given set of data :

x : 1 2 3 4 5 6

y : 4.05 7.12 9.65 12.20 15.20 19.00 4

(c) What do you mean by Regression Analysis. 4

3. (a) Explain what is non-linear regression. 4

(b) Fit an exponential curve to the following data :

x : 0.4 0.8 1.2 1.6 2 2.3

y : 800 975 1500 1950 2900 3600 4

(c) Explain what is transcendental equation ? Explain the method to fit transcendental equation. 4

**OR**

4. (a) Fit a second degree curve  $y = a + bx + cx^2$  to the following data relating to profit in a year of certain company.

Year (x)	: 1980	1982	1984	1986	1988
(y)	: 125	140	165	195	230

Estimate the profit in the year 1995. 4

(b) How will you reduce non-linear equation in linear form ? 4

(c) Explain the method for fitting of the polynomial functions to the given data. 4

5. (a) State Newton's Gregory forward interpolation formula. In which case is it useful ? 6

(b) The population of a country in the decennial census was as under. Estimate the population for the year 1925 :

Year (x)	: 1891	1901	1911	1921	1931
Population in thousands (y)	: 46	66	81	93	101

6

**OR**

6. (a) Derive Lagrange's interpolation formula. 6

(b) Using Newton's divided difference formula, find the value of y corresponding to  $x = 10$  from the following table :

x	: 5	6	9	11
y	: 12	13	14	16

6

7. (a) Explain inverse interpolation technique. 4

(b) Explain the spline interpolation technique. 4

(c) Apply Lagrange's formula inversely to find the age for which the annuity value is 13.6, given the following table :

Age x	: 30	35	40	45	50
A.V.	: 15.9	14.9	14.1	13.3	12.5

4

**OR**

8. (a) What are the different assumptions of inverse interpolation ? 4

(b) Explain the Chebyshev interpolation polynomial. 4

(c) Obtain a value of  $x$  where  $y_x = 19$ . Given the following values :

$x$	:	0	1	2
$f(x)$	:	0	1	20

4

9. (a) Obtain Simpson's  $1/3^{\text{rd}}$  rule by using general quadrature formula. Evaluate :

$$\int_0^3 \cos^2 x \, dx, \quad b=6,$$

6

(b) State and prove trapezoidal rule of numerical integration.

6

OR

10. (a) Evaluate :

$$\int_0^1 \frac{dx}{1+x} \text{ approximately in step of } 0.25 \text{ by}$$

(i) Trapezoidal rule

(ii) Simpson's  $3/8^{\text{th}}$  rule.

6

(b) State general quadrature formula for numerical integration.

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