

B. Pharm Second Semester
35148 : Mathematics - 2.6

P. Pages : 2

Time : Three Hours



AU - 0663

Max. Marks : 60

- Notes : 1. All question carry equal marks.
 2. Answer **any five** question from given seven Questions.
 3. Use of calculator is permissible.
 4. Use of pen Blue/Black ink/refill only for writing the answer book.

1. a) Attempt **any two** of the following.

a) The area of circle is 36π sq.cm find the angle made by an arc of length 8 cm at the centre of circle in degree measure. 3

b) Prove that $\sin^2 A + \cos^4 A = \cos^2 A + \sin^4 A$ 3

c) If $\cos 0 = 0.4$ find the value of $\cos 30$. 3

b) Evaluate **any one** of the following.

a) Find $\lim_{x \rightarrow \pi/3} \frac{\sqrt{3} - \tan x}{\pi - 3x}$ 6

b) Prove that $\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} = n \cdot a^{n-1}$ 6

2. Evaluate **any three** of the following.

a) Find $\frac{dy}{dx}$ if $y = \log \left[\frac{\sin x}{1 + \cos x} \right]$ 4

b) Discuss continuity of 4

$$f(x) = \frac{12^x - 4^x - 3^x + 1}{x^2}, \quad x \neq 0 \\ = \log 12, \quad x = 0 \quad \text{at } x = 0$$

c) Find $\frac{dy}{dx}$ if $y = \frac{1 - \sqrt{x}}{1 + \sqrt{x}}$ 4

d) Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{a+x} - \sqrt{a-x}}{x}$ 4

3. Attempt **any three** of the following.

a) If $x^y = e^{x-y}$ then show that $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$ 4

b) Evaluate $\int x \cdot \sec^2 x \cdot dx$ 4

- c) Differentiate x^3 using first principle of derivative. 4
- d) Evaluate $\int (\tan x + \cot x)^2 dx$ 4
- 4.** Evaluate any two of the following. 6
- a) If $0 \leq x \leq 2a$ then prove that $\int_0^{2a} f(x) dx = \int_0^a f(x) dx + \int_0^a f(2a-x) dx$ 6
- b) Solve the differential equation $(x-y) \cdot \frac{dy}{dx} = x+y$ 6
- c) Show that $y = x^2 \cdot e^x$ is solution of differential equation 6
- $$x^2 \frac{d^2y}{dx^2} - x^2 \frac{dy}{dx} - 2y \cdot (x+1) = 0$$
- 5.** Evaluate any three of the following. 12
- a) A die is thrown find the probability of getting
 i) a prime Number ii) A multiple of 3 4
- b) Tickets numbered 1 to 20 are mixed together and one ticket is drawn at random find the probability that ticket is of numbered multiple of 3 or 7. 4
- c) Write notes on Pie – diagram. 4
- d) Discuss in brief the Histogram. 4
- 6.** Attempt any two of the following. 12
- a) The Mean and S. D. of x are 36 and 4.6 and that of y are 49 and 7.3 find the equation of two lines of regression if coefficient of correlation 0.75. 6
- b) Find the mode and median of following data. 6
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|-------|---------|----------|-----------|-----------|-----------|-----------|
| Class | 60 – 90 | 90 – 120 | 120 – 150 | 150 – 180 | 180 – 210 | 210 – 240 |
| Freq. | 12 | 23 | 43 | 27 | 18 | 14 |
- c) If θ is an acute angle between the two lines of regression then prove that 6
- $$\tan \theta = \frac{1 - \gamma}{\gamma^2 - \frac{\sigma x \cdot \sigma y}{\sigma x^2 + \sigma y^2}}$$
- 7.** Evaluate any one of the following. 12
- a) Find mean and coefficient of variance for following data using step deviation method. 12
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|-------|---------|---------|---------|---------|---------|---------|---------|
| Class | 100–150 | 150–200 | 200–250 | 250–300 | 300–350 | 350–400 | 400–450 |
| Freq. | 25 | 75 | 125 | 175 | 125 | 85 | 60 |
- b) Find the equation of line of regression of x on y for following data. 12
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|---|-----|-----|-----|-----|-----|----|-----|----|----|----|
| x | 105 | 104 | 102 | 101 | 100 | 99 | 98 | 96 | 93 | 92 |
| y | 101 | 103 | 100 | 98 | 97 | 96 | 104 | 92 | 97 | 94 |